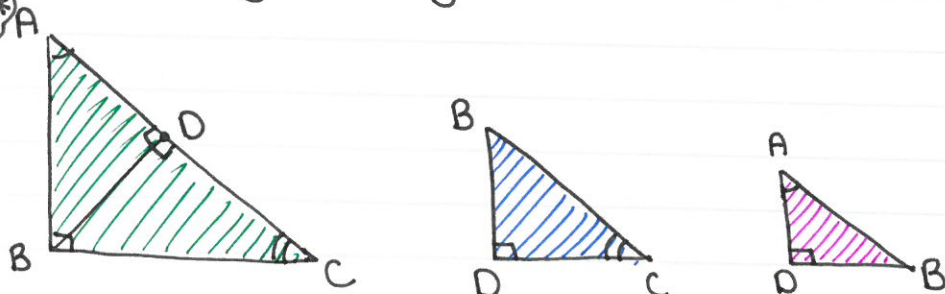


4A.6 - Using Triangle Similarity in Right Triangles

Unit 4A
day 6

Activity



$$\triangle ABC \sim \triangle BDC \sim \triangle ADB$$

thm: the altitude to the hypotenuse of a right triangle into two triangles that are similar to the original \triangle and to each other.

Ratios created:

$$\frac{AD}{BD} = \frac{BD}{CD}$$

$$\frac{BC}{CA} = \frac{DC}{BC}$$

$$\frac{AB}{AD} = \frac{AC}{AB}$$

* Geometric Mean
x is geometric mean of a & b

if $\frac{a}{x} = \frac{x}{b}$ or $x^2 = ab$

$$x = \pm \sqrt{ab}$$

each of the above has a geometric mean!!

ex: Find the geometric mean of 2 and 8.

$$\frac{2}{x} = \frac{x}{8}$$

$$x = \pm 4$$

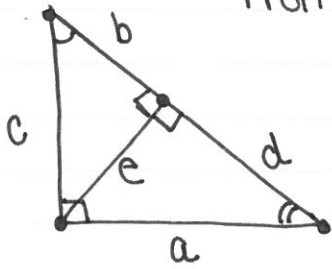
ex. Find the geometric mean of 4 and 9.

$$\frac{4}{x} = \frac{x}{9}$$

$$x = \pm 6$$

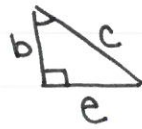
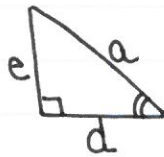
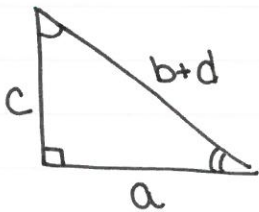
U4.6

From previous page:

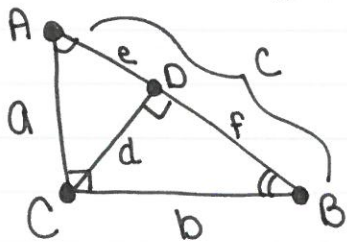


$$\frac{b}{c} = \frac{c}{b+d} \quad \frac{b}{e} = \frac{e}{d}$$

$$\frac{d}{a} = \frac{a}{d+b}$$



So fascinating:



$$\triangle ABC \sim \triangle CBD$$

$$\triangle ABC \sim \triangle ACD$$

Given

$$\frac{a}{c} = \frac{e}{a} \quad \therefore \quad \frac{b}{f} = \frac{c}{b}$$

Corr. sides of similar Δ 's are proportional.

$$a^2 = ce \quad \text{and} \quad b^2 = cf$$

Cross product property

$$\begin{aligned} a^2 &= ce \\ + b^2 &= cf \\ \hline a^2 + b^2 &= ce + cf \end{aligned}$$

add. p.o.e

$$a^2 + b^2 = c(e+f)$$

distributive

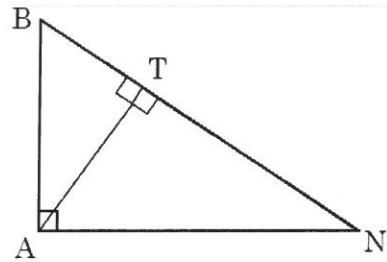
$$c = e + f$$

seg add post.

$$a^2 + b^2 = c^2$$

substitution

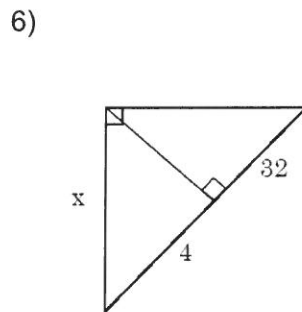
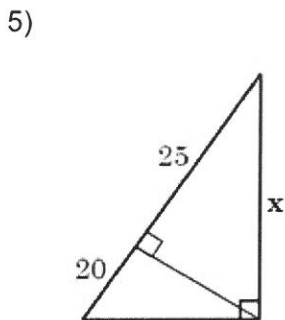
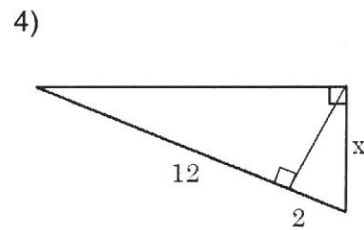
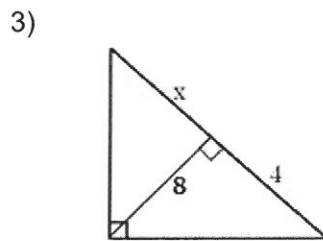
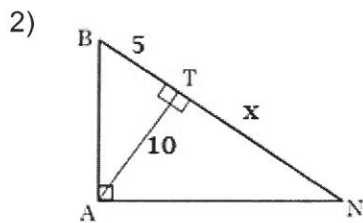
1) If an altitude is drawn to the hypotenuse of triangle BAN below, then name and redraw the 3 similar triangles created.



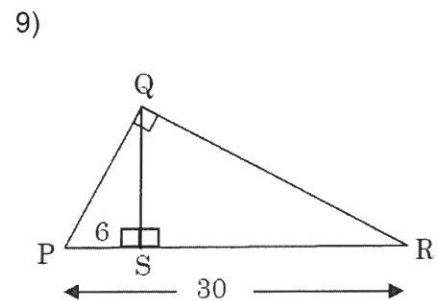
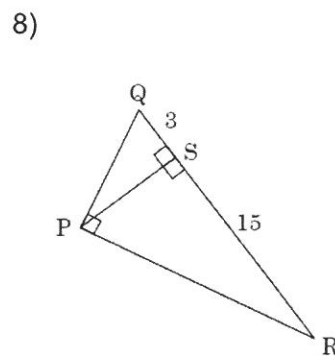
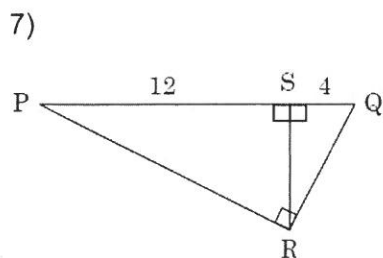
Write the similarity statement comparing the three triangles

$\Delta \underline{\hspace{1cm}} \sim \Delta \underline{\hspace{1cm}} \sim \Delta \underline{\hspace{1cm}}$

Determine the missing value "x" below:



For 7-9 Set up and solve for the length of the altitude of right triangle PQR.



Determine the geometric mean of the following numbers.

10) 5 and 8

11) 7 and 11

12) 4 and 9

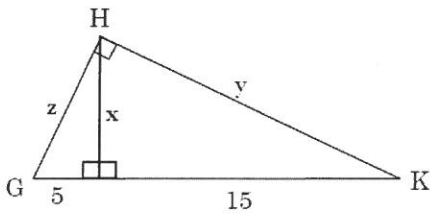
13) 2 and 25

14) 6 and 8

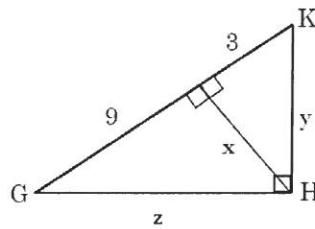
15) 8 and 32

Solve for the variables x , y , and z in each triangle.

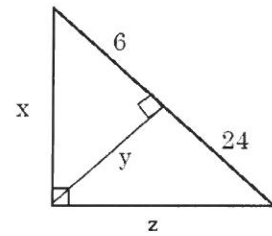
16)



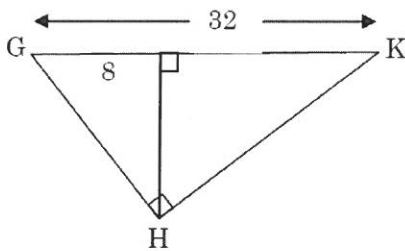
17)



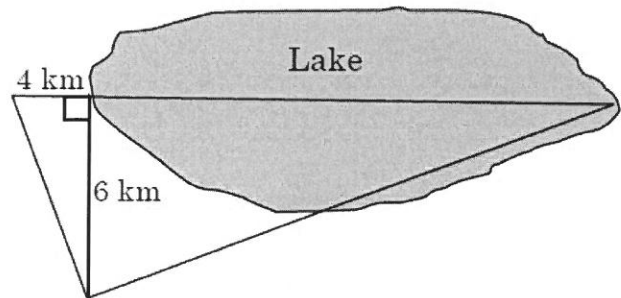
18)



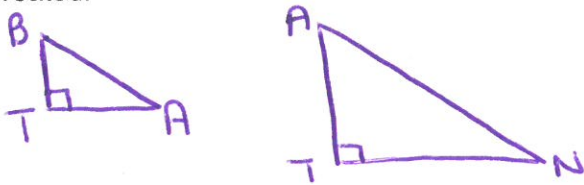
19) Determine the lengths of GH and HK .



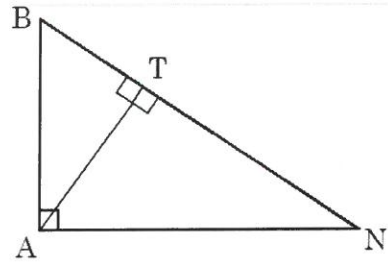
20) Determine the distance across the lake?



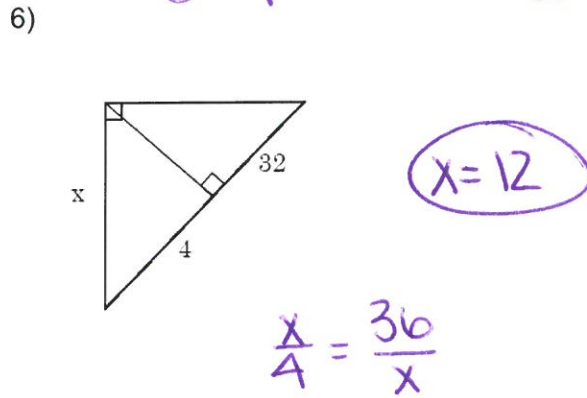
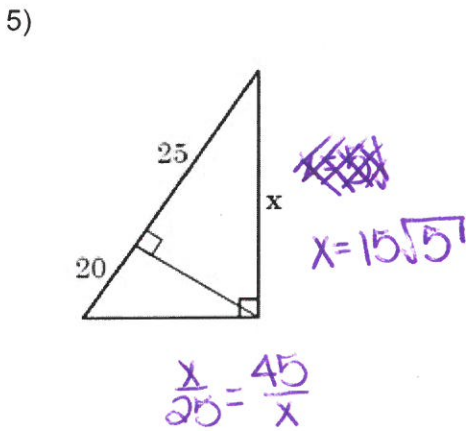
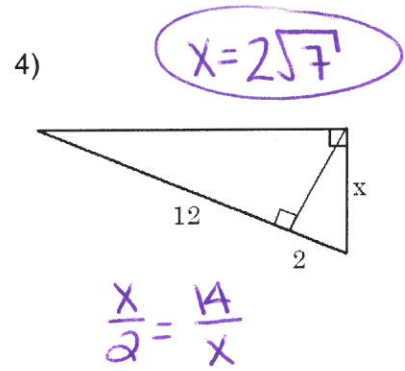
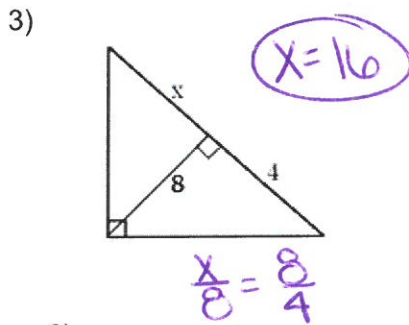
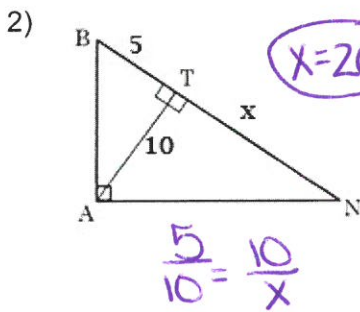
1) If an altitude is drawn to the hypotenuse of triangle BAN below, then name and redraw the 3 similar triangles created.



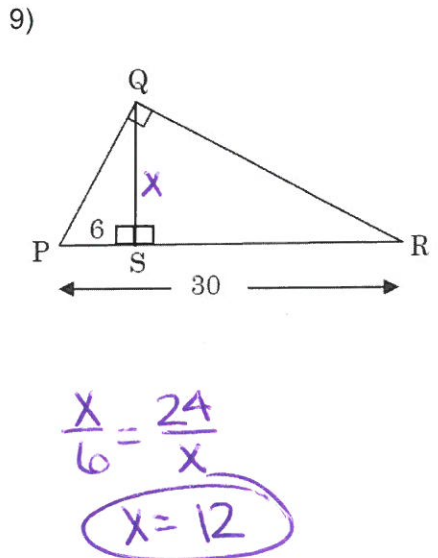
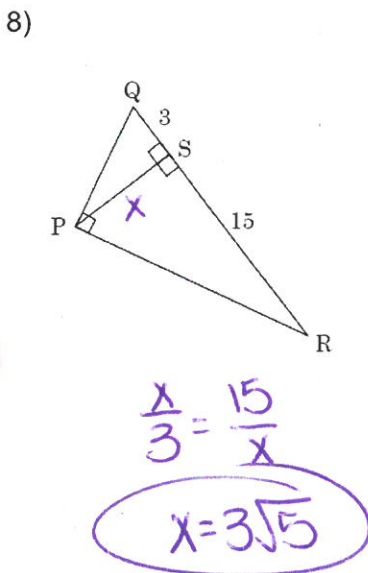
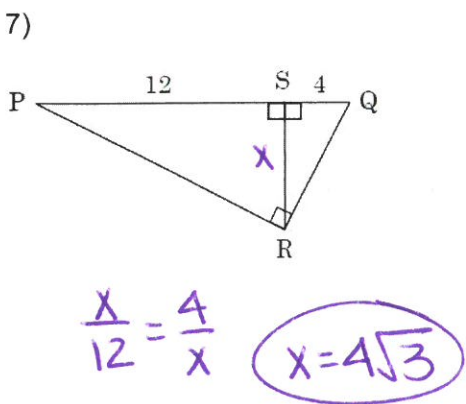
Write the similarity statement comparing the three triangles
 $\Delta BTA \sim \Delta ATN \sim \Delta BAN$



Determine the missing value "x" below:



For 7-9 Set up and solve for the length of the altitude of right triangle PQR.



Determine the geometric mean of the following numbers.

10) 5 and 8

$$\pm 2\sqrt{10}$$

11) 7 and 11

$$\pm \sqrt{77}$$

12) 4 and 9

$$\pm 6$$

13) 2 and 25

$$\pm 5\sqrt{2}$$

14) 6 and 8

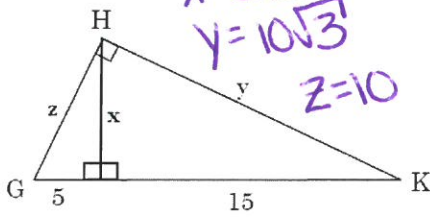
$$\pm 4\sqrt{3}$$

15) 8 and 32

$$\pm 16$$

Solve for the variables x, y, and z in each triangle.

16)



$$x = 5\sqrt{3}$$

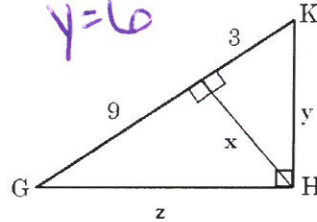
$$y = 10\sqrt{3}$$

$$z = 10$$

$$\frac{x}{5} = \frac{15}{x} \quad \frac{5}{z} = \frac{z}{20}$$

$$\frac{y}{15} = \frac{20}{y}$$

17)



$$x = 3\sqrt{3}$$

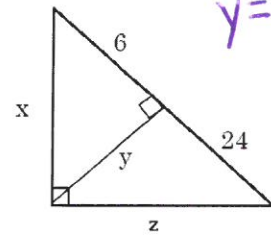
$$y = 6$$

$$z = 6\sqrt{3}$$

$$\frac{x}{9} = \frac{3}{x} \quad \frac{z}{9} = \frac{12}{z}$$

$$\frac{y}{3} = \frac{12}{y}$$

18)



$$z = 12\sqrt{5}$$

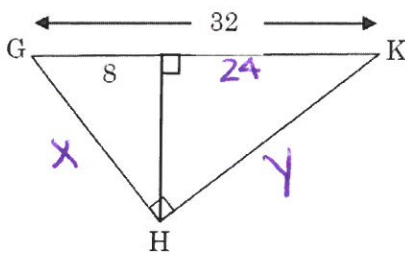
$$x = 6\sqrt{5}$$

$$y = 12$$

$$\frac{y}{6} = \frac{24}{y} \quad \frac{z}{24} = \frac{30}{z}$$

$$\frac{x}{6} = \frac{30}{x}$$

19) Determine the lengths of GH and HK.

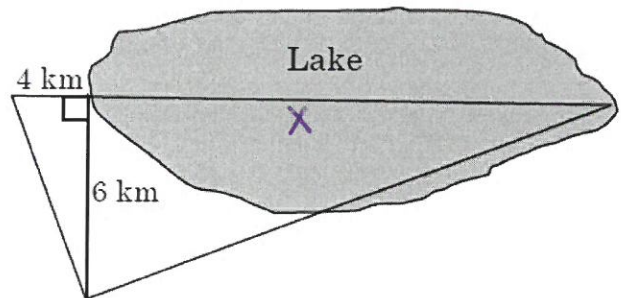


$$\frac{x}{8} = \frac{40}{x} \quad \frac{y}{24} = \frac{32}{y}$$

$$x = 8\sqrt{5}$$

$$y = 16\sqrt{3}$$

20) Determine the distance across the lake?



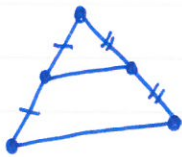
$$\frac{6}{4} = \frac{x}{6}$$

$$4x = 36$$

$$x = 9$$

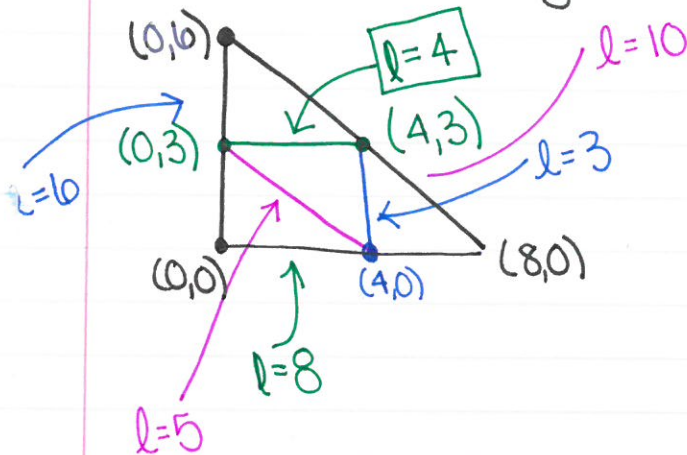
Triangle Midsegment

def'n: a segment connecting the midpoints of 2 sides of a Δ



theorem: if a segment joins the midpoints of 2 sides of a Δ , then the segment is parallel to the third side and half its length.

ex: ΔABC has vertices $A(0,6)$ $B(8,0)$ and $C(0,0)$.
Find the midpoints of each side.
Find the length of each side.
Find the length of each midsegment



$$l = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$(4,0)$ to $(0,3)$

$$l = \sqrt{(4-0)^2 + (0-3)^2}$$

$$l = \sqrt{16+9}$$

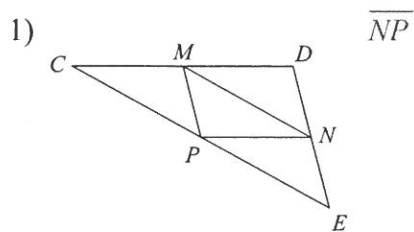
$$l = 5$$

do slopes support parallel-ness?

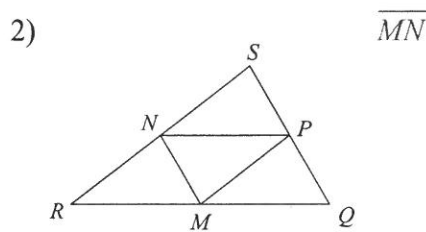
yes

Midsegment of a Triangle

In each triangle, M, N, and P are the midpoints of the sides. Name a segment parallel to the one given.



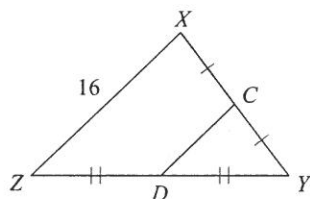
$\overline{CD} \parallel$ _____



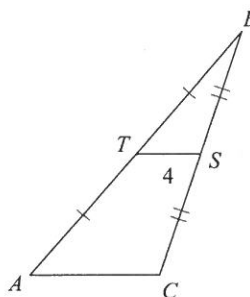
_____ $\parallel \overline{QS}$

Find the missing length indicated.

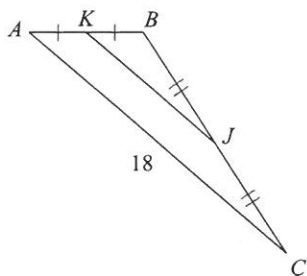
3) Find CD 8



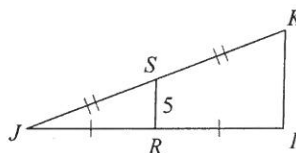
4) Find AC 8



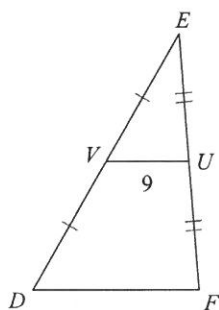
5) Find KJ 9



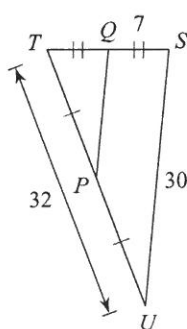
6) Find IK 10



7) Find DF 18

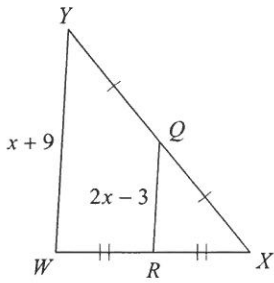


8) Find PQ 15



Solve for x .

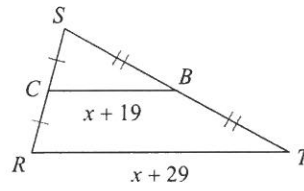
9)



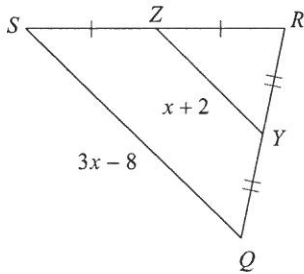
5

10)

-9



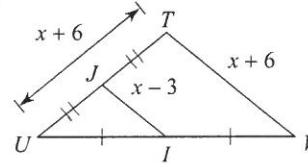
11)



12

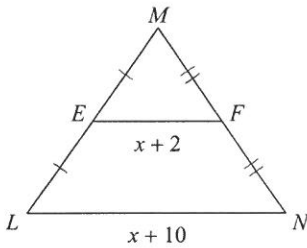
12)

12



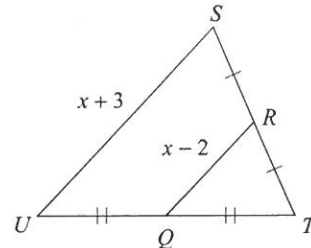
Find the missing length indicated.

13) Find LN



16

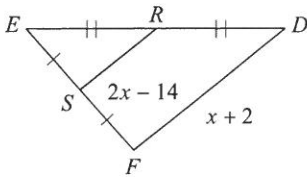
14) Find RQ



5

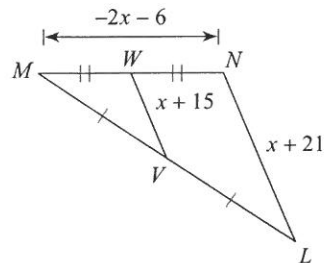
15) Find SR

6



16) Find VW

6



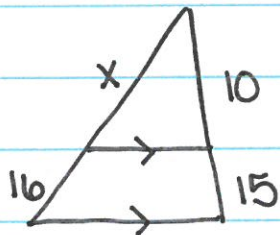
4A.8 - Triangle Proportionality Thm.

Unit 4A
day 8

Side Splitter Theorem:

If a line is parallel to one side of a triangle and intersects the other two sides, then it divides those sides proportionally.

ex: find the value of x .



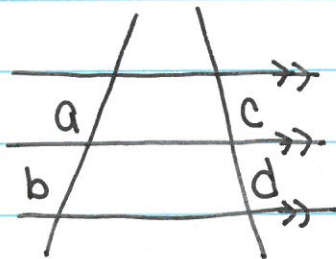
$$\frac{x}{16} = \frac{10}{15}$$

$$15x = 160$$

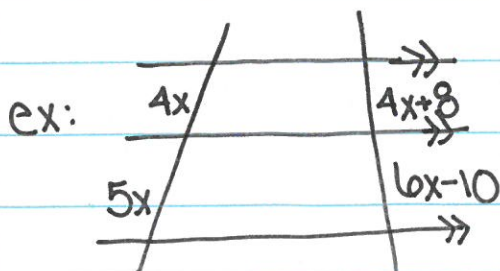
$$x = 10\frac{2}{3}$$

Side Splitter Corollary:

If 3 parallel lines intersect 2 transversals, then the segments intercepted on those transversals are proportional.



$$\frac{a}{b} = \frac{c}{d}$$



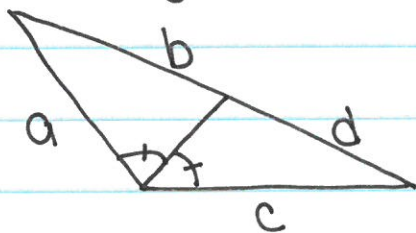
$$\frac{4x}{5x} = \frac{4x+8}{6x-10}$$

$$4(6x-10) = 5(4x+8)$$

$$4x = 80 \quad \boxed{x=20}$$

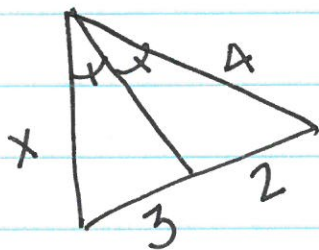
Triangle-Angle-Bisector Thm

If a ray bisects an angle of a triangle, then it divides the opposite side into two segments that are proportional to the other two sides of the triangle.



$$\frac{a}{b} = \frac{c}{d}$$

ex.



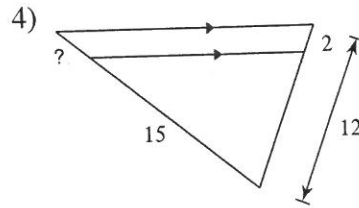
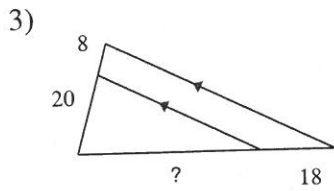
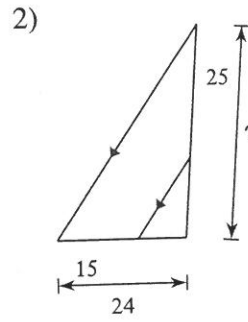
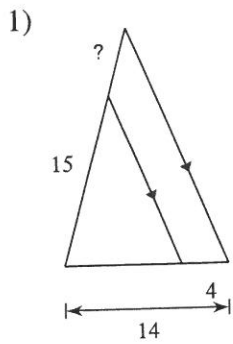
$$\frac{x}{3} = \frac{4}{2}$$

$$2x = 12$$

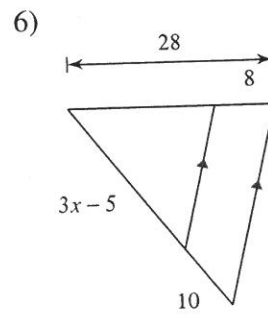
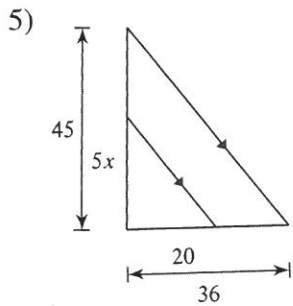
$$x = 6$$

Proportional Parts in Triangles and Parallel Lines

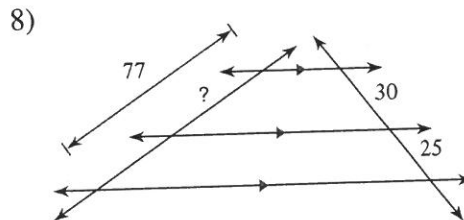
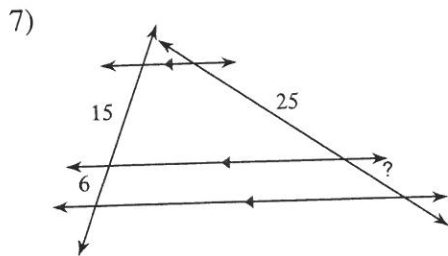
Find the missing length indicated.



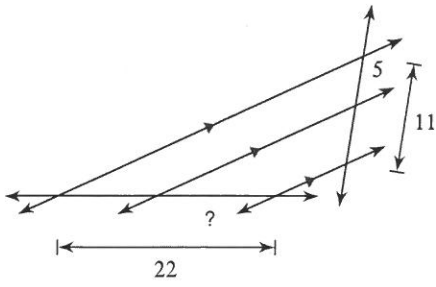
Solve for x .



Find the missing length indicated.

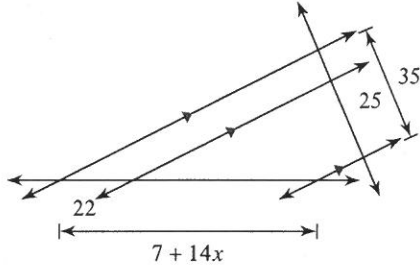


9)



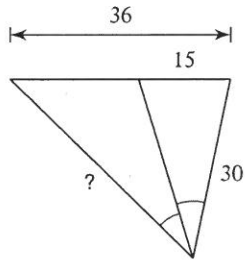
Solve for x .

11)

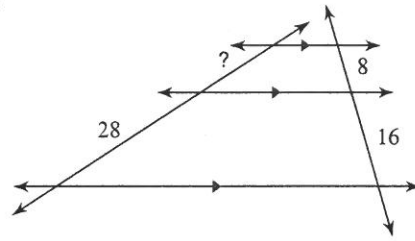


Find the missing length indicated.

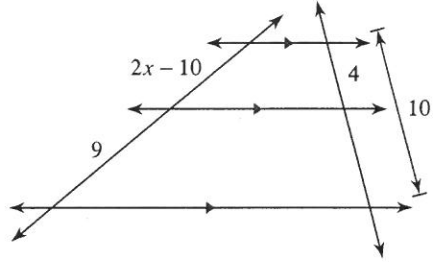
13)



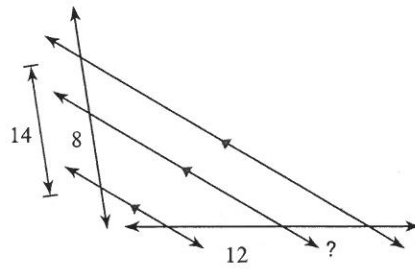
10)



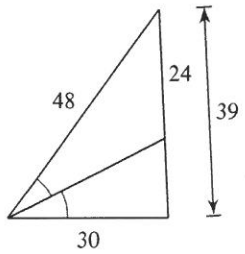
12)



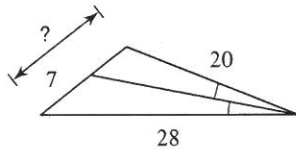
14)



15)

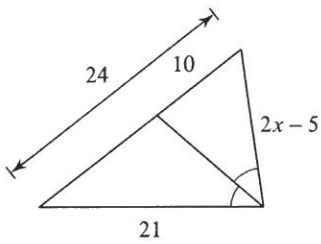


16)

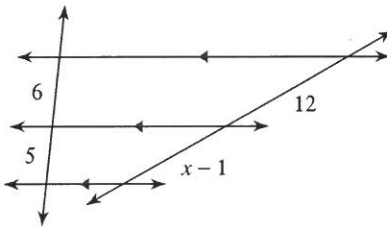


Solve for x .

17)

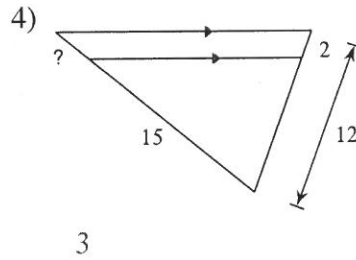
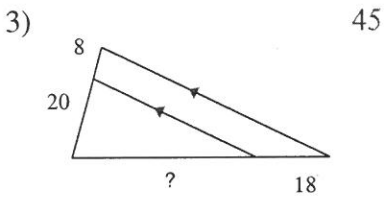
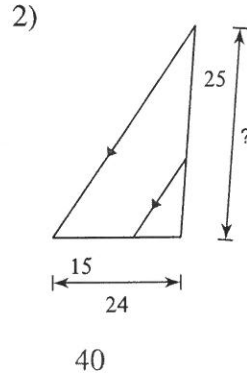
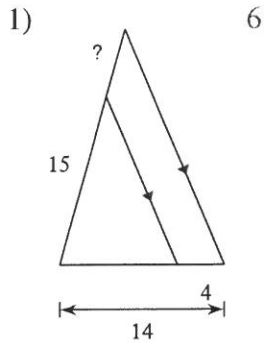


18)

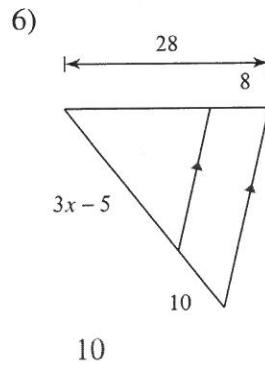
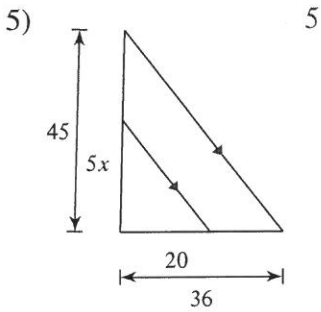


Proportional Parts in Triangles and Parallel Lines

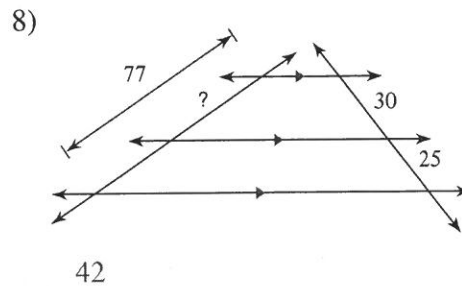
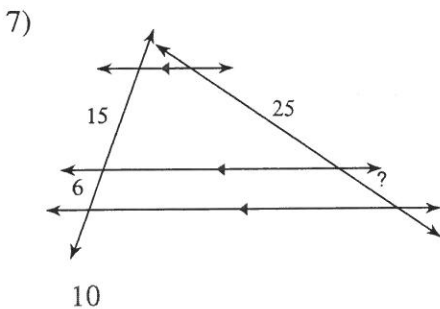
Find the missing length indicated.

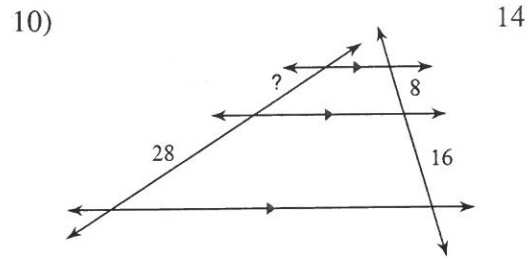
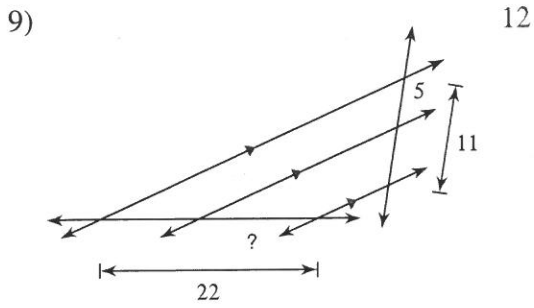


Solve for x .

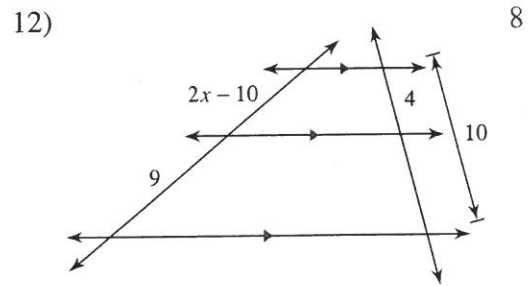
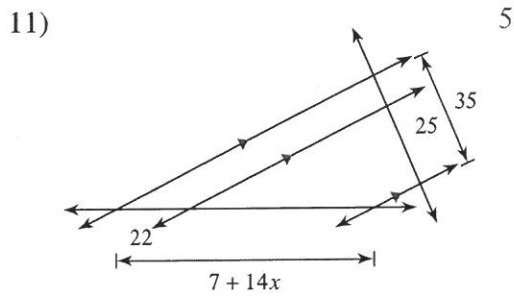


Find the missing length indicated.

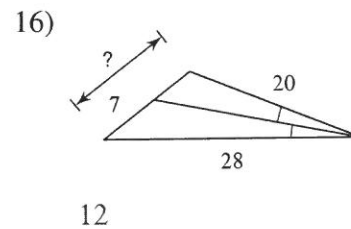
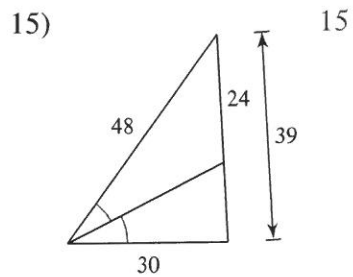
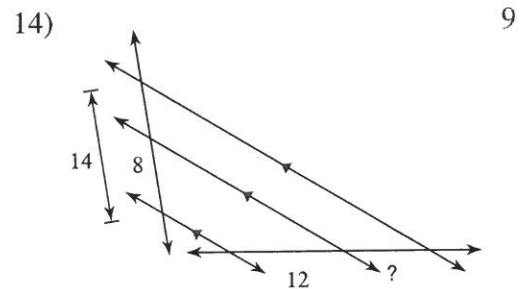
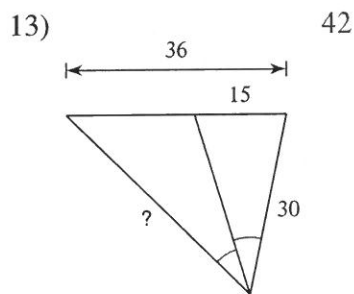




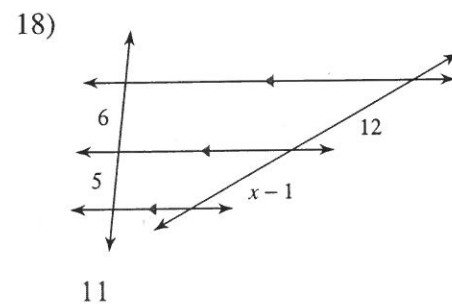
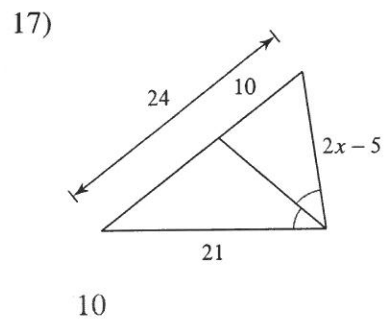
Solve for x .

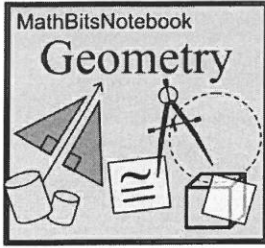


Find the missing length indicated.



Solve for x .



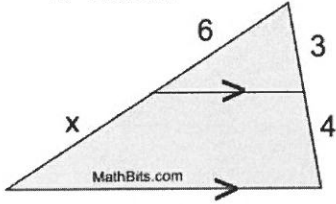


Side Splitter Theorem Practice

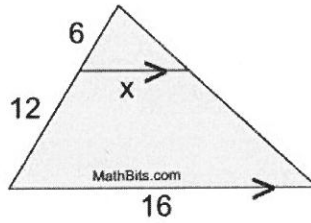
Name _____ **ANSWERS**

Directions: Read carefully. Please show your work.

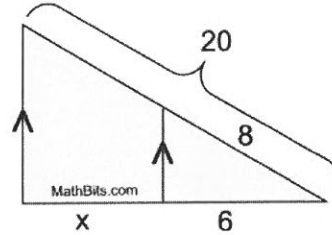
1. Find x .



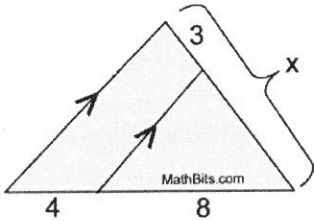
2. Find x .



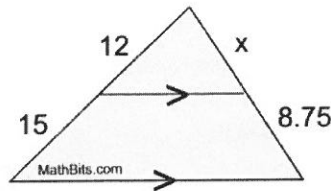
3. Find x .



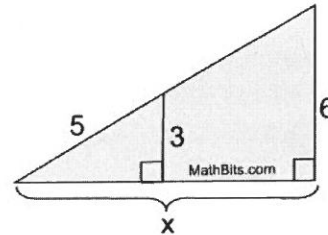
4. Find x .



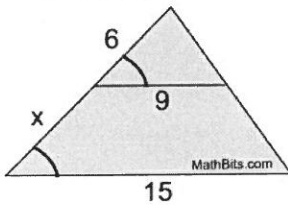
5. Find x .



6. Find x .

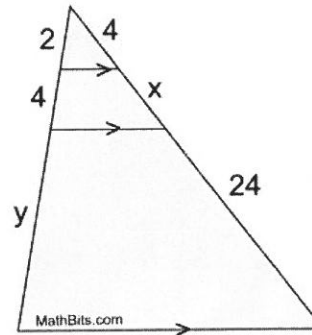


7. Find x .

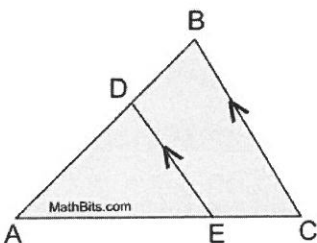


8. a) Find x .

b) Find y .



9. If $AB = AC$, which choice is FALSE?

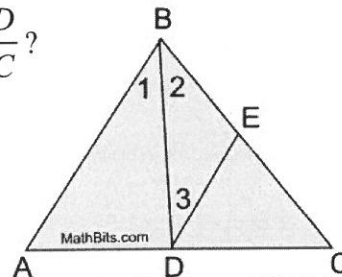


- (1) $AD = AE$
- (2) $DB = EC$
- (3) $\frac{AD}{DB} = \frac{AE}{EC}$
- (4) $\frac{AD}{AE} = \frac{DE}{BC}$

10. Given: \overline{BD} bisects $\angle ABC$; $BE = ED$

Is $\frac{BE}{EC} = \frac{AD}{DC}$?

Explain.



ANSWERS

1. 8

2. $5\frac{1}{3}$

3. 9

4. 9

5. 7

6. 8

7. 4

8.a. 8

b. 12

9. (4)

10. Yes

The \angle bisector gives $\angle 1 \cong \angle 2$. If $BE = ED$, $\triangle BED$ is isosceles, making base angles congruent, $\angle 2 \cong \angle 3$. By transitive property, $\angle 1 \cong \angle 3$. With \cong alternate interior \angle s, $\overline{AB} \parallel \overline{DE}$. Side Splitter Th^m gives proportion true.